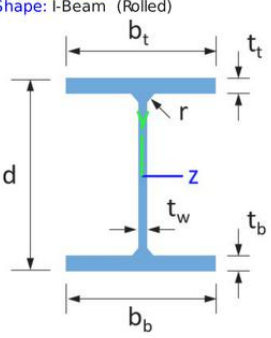


REFERENCES	CALCULATIONS	RESULTS
<p>Code: AISC 360-16 LRFD</p>	<p><b>MEMBER #1 DESIGN REPORT</b></p> <p><b>Project details</b></p> <p>Project Name:  Project ID:  Company:  Designer:  Client:  Project Notes:  Project Units: imperial</p> <p><b>General member design information</b></p> <p>Section Name: W8x58  Shape: I-Beam (Rolled)</p>  <p><b>Dimensions:</b>  Height <math>d = 8.750</math> in  Web Thick <math>t_w = 0.510</math> in  Top Flange Width <math>b_t = 8.220</math> in  Top Flange Thick <math>t_t = 0.810</math> in  Bottom Flange Width <math>b_b = 8.220</math> in  Bottom Flange Thick <math>t_b = 0.810</math> in  Fillet <math>r = 0.390</math> in</p> <p><b>Properties:</b>  Area <math>A = 17.100</math> in<sup>2</sup>  Moment of Inertia about the z-axis <math>I_z = 228.000</math> in<sup>4</sup>  Moment of Inertia about the y-axis <math>I_y = 75.100</math> in<sup>4</sup>  Plastic Section Modulus about the z-axis <math>Z_z = 59.3478</math> in<sup>3</sup>  Plastic Section Modulus about the y-axis <math>Z_y = 27.829</math> in<sup>3</sup>  Torsion Contant <math>J = 3.330</math> in<sup>4</sup>  Warping Contant <math>I_w = 1168.250</math> in<sup>6</sup></p> <p><b>Material properties:</b>  Material Name: Structural Steel  Modulus of Elasticity <math>E = 29000</math> ksi  Yield Strength <math>F_y = 38</math> ksi  Ultimate Tensile Strength <math>F_u = 60</math> ksi</p> <p><b>Design parameters:</b>  Member length <math>L = 10.000</math> ft  Length between braced points <math>L_b = 10.000</math> ft  Effective Length factor for flexural buckling about y-axis <math>K_y = 2.100</math>  Effective Length factor for flexural buckling about z-axis <math>K_z = 2.100</math></p> <p><b>Load case</b></p> <p>Axial Force <math>P = 5.000</math> kip  Major Bending Moment <math>M_z = 86.243</math> kip-ft  Minor Bending Moment <math>M_y = 0.000</math> kip-ft  Shear Force <math>V_z = 0.000</math> kip  Shear Force <math>V_y = 15.582</math> kip</p>	
	<p><b>CHECK AXIAL STRENGTH (axial compression member)</b></p> <p>Check slenderness ratio of axial compression member (AISC E2)</p> <p>Slenderness ratio z-axis</p> $\lambda_z = \frac{K_z L}{r_z} = \frac{21.000}{0.304} = 69.013$ <p>Slenderness ratio y-axis</p> $\lambda_y = \frac{K_y L}{r_y} = \frac{21.000}{0.175} = 120.249$	

Maximum slenderness ratio

$$\lambda = \max(\lambda_y, \lambda_z) = \max(69.013, 120.249) = 120.249$$

$$\lambda = 120.249 < 200$$

STATUS OK!

Check width-thickness ratio of flange (B4. Table B4.1a)

$$\lambda_f = \frac{0.5 \cdot b_f}{t_f} = \frac{0.5 \cdot 8.220}{0.810} = 5.074$$

$$\lambda_{r_f} = 0.56 \sqrt{\frac{E_s}{F_y}} = 0.56 \sqrt{\frac{29000}{38}} = 15.470$$

$$\lambda_f = 5.074 < \lambda_{r_f} = 15.470 \rightarrow \text{non-slender section}$$

$$\lambda_w = \frac{d - t_f - t_b - 2r}{t_w} = \frac{8.750 - 0.810 - 0.810 - 2 \cdot 0.390}{0.510} = 12.451$$

$$\lambda_{r_w} = 1.49 \sqrt{\frac{E_s}{F_y}} = 1.49 \sqrt{\frac{29000}{38}} = 41.162$$

$$\lambda_w = 12.451 < \lambda_{r_w} = 41.162 \rightarrow \text{non-slender section}$$

#### Calculate Flexural Buckling Stress

Calculate the elastic critical buckling stress  $F_c$ .

$$F_c = \frac{\pi^2 E}{\lambda^2} = \frac{\pi^2 \cdot 29000}{120.248^2} = 19.794 \text{ ksi}$$

Calculate the flexural buckling stress  $F_{cr}$ .

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{29000}{38}} = 130.115$$

Because:

$$\lambda = 120.248 < 130.115$$

$$F_{cr} = [0.658 \frac{F_y}{F_c}] F_y = [0.658 \frac{38}{19.794}] \cdot 38 = 17.015 \text{ ksi}$$

Nominal Compressive Strength  $P_n$ .

$$P_n = F_{cr} A_g = 17.015 \cdot 17.100 = 290.951 \text{ kip}$$

Calculate axial compressive strength.

Resistance factor for compression:  $\phi_c = 0.900$

$$\phi_c P_n = 0.900 \cdot 290.951 = 261.856 \text{ kip}$$

Calculate the flexural buckling stress  $F_{cr}$ .

$$4.71 \sqrt{\frac{E}{F_y}} = 4.71 \sqrt{\frac{29000}{38}} = 130.115$$

Because:

$$\lambda = 120.248 < 130.115$$

$$F_{cr} = [0.658 \frac{F_y}{F_c}] F_y = [0.658 \frac{38}{19.794}] \cdot 38 = 17.015 \text{ ksi}$$

Check ratio of axial strength  $\frac{P}{\phi_c P_n}$

$$\frac{P}{\phi_c P_n} = \frac{5.000}{261.856} = 0.019 < 1.0$$

STATUS OK!

### CHECK FLEXURAL STRENGTH ABOUT MAJOR AXIS

Calculate limiting width-thickness ratio of flange for flexure (AISC B4, Table B4.1b)

$$\lambda_f = \frac{0.5 \cdot b_f}{t_f} = \frac{0.5 \cdot 8.220}{0.810} = 5.074$$

$$\lambda_{pf} = 0.38 \sqrt{\frac{E}{F_y}} = 0.38 \sqrt{\frac{29000}{38}} = 10.498$$

$$\lambda_{rf} = 1.00 \sqrt{\frac{E}{F_y}} = 1.00 \sqrt{\frac{29000}{38}} = 27.625$$

$$\lambda_f = 5.074 < \lambda_{pf} = 10.498 \rightarrow \text{COMPACT}$$

Calculate limiting width-thickness ratio of web for flexure

$$\lambda_w = \frac{d - tt - tb - 2r}{t_w} = \frac{8.750 - 0.810 - 0.810 - 2 \cdot 0.390}{0.510} = 12.451$$

$$\lambda_{pw} = 3.76 \sqrt{\frac{E}{F_y}} = 3.76 \sqrt{\frac{29000}{38}} = 103.871$$

$$\lambda_{rw} = 5.70 \sqrt{\frac{E}{F_y}} = 5.70 \sqrt{\frac{29000}{38}} = 157.464$$

$$\lambda_w = 12.451 < \lambda_{pw} = 103.871 \rightarrow \text{COMPACT}$$

Calculate lateral-torsional buckling modification factor

$$C_b = 2.230$$

### Yielding

Calculate nominal flexural strength for Yielding (AISC F2.1 (F2-1))

$$M_{n1} = M_p = F_y Z_x = 38.000 \cdot 59.348 = 187.18300141350002 \text{ k-ft}$$

### Lateral-Torsional Buckling

Compute limiting laterally unbraced length for the limit state of yielding F2.2 (F2-5)

$$L_p = 1.76 r_y \sqrt{\frac{E}{F_y}} = 1.76 \cdot 2.096 \cdot \sqrt{\frac{29000}{38}} = 101.892 \text{ in}$$

Laterally unbraced length for the limit state of inelastic lateral-torsional buckling F2.2 (F2-6)  
For doubly symmetric I-shapes F2-8a

$$c = 1.00$$

Distance between the flange centroid

$$h_0 = d - 0.5(tt + tb) = 8.750 - 0.5(0.810 + 0.810) = 7.940 \text{ in}$$

$$r_{ts} = \sqrt{\frac{I_y C_w}{S_z^2}} = \sqrt{\frac{75.100 \cdot 1168.250}{52.114^2}} = 2.384 \text{ in}$$

$$L_r = 1.95 r_{ts} \frac{E}{0.7 F_y} \sqrt{\frac{Jc}{S_z h_0} + \sqrt{\left(\frac{Jc}{S_z h_0}\right)^2 + 6.76 \left(\frac{0.7 F_y}{E}\right)^2}}$$



$$u_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad u_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Orthogonal basis for  $W_1$ :

$$u_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_2$ :

$$u_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$u_3 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_3$ :

$$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

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Orthogonal basis for  $W_4$ :

Orthogonal basis for  $W_1$ :

$$u_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_2$ :

$$u_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$u_3 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_3$ :

$$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

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Orthogonal basis for  $W_4$ :

Orthogonal basis for  $W_1$ :

$$u_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_2$ :

$$u_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad u_3 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}, \quad u_4 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$u_5 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Orthogonal basis for  $W_3$ :

$$u_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_4$ :

$$u_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$u_3 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Orthogonal basis for  $W_5$ :

$$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad \frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

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1. (a) (i)  $2x^2 + 3x - 5$  (ii)  $3x^2 - 2x + 1$  (iii)  $4x^2 - 5x + 2$